



# SAD: Semi-Supervised Anomaly Detection on Dynamic Graphs

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Code&data: <https://github.com/D10Andy/SAD>.



Reported by Nengqiang Xiang

# Introduction

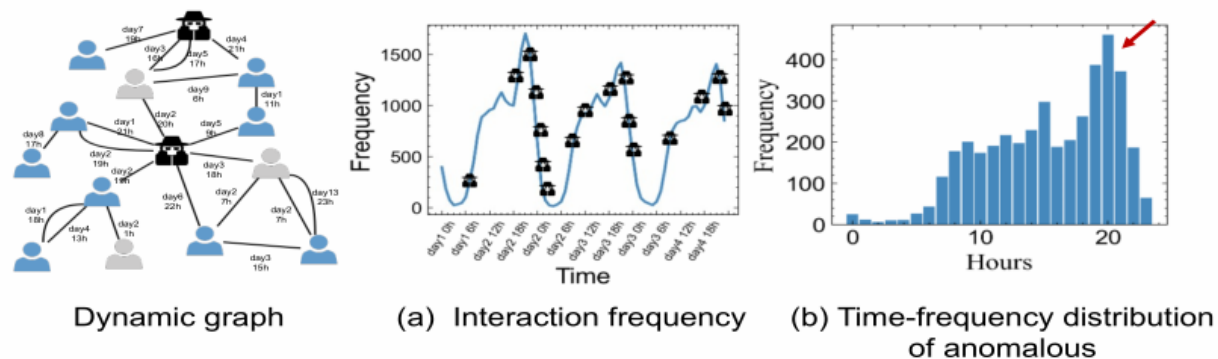


Figure 1: Statistical distribution of evolving graph streams on the MOOC dataset. **Observations:** (a) The frequency of interactions shows a clear cyclical pattern on the time axis. (b) Anomalous samples typically occurred between 8 am and 10 pm, with peaks at around 8 pm.

Existing methods are two limitations:  
Underutilization of unlabeled data; Lack of dynamic information mining.

In this paper, the author presents semi-supervised anomaly detection (SAD), an end-to-end framework for anomaly detection on dynamic graphs.

## Method

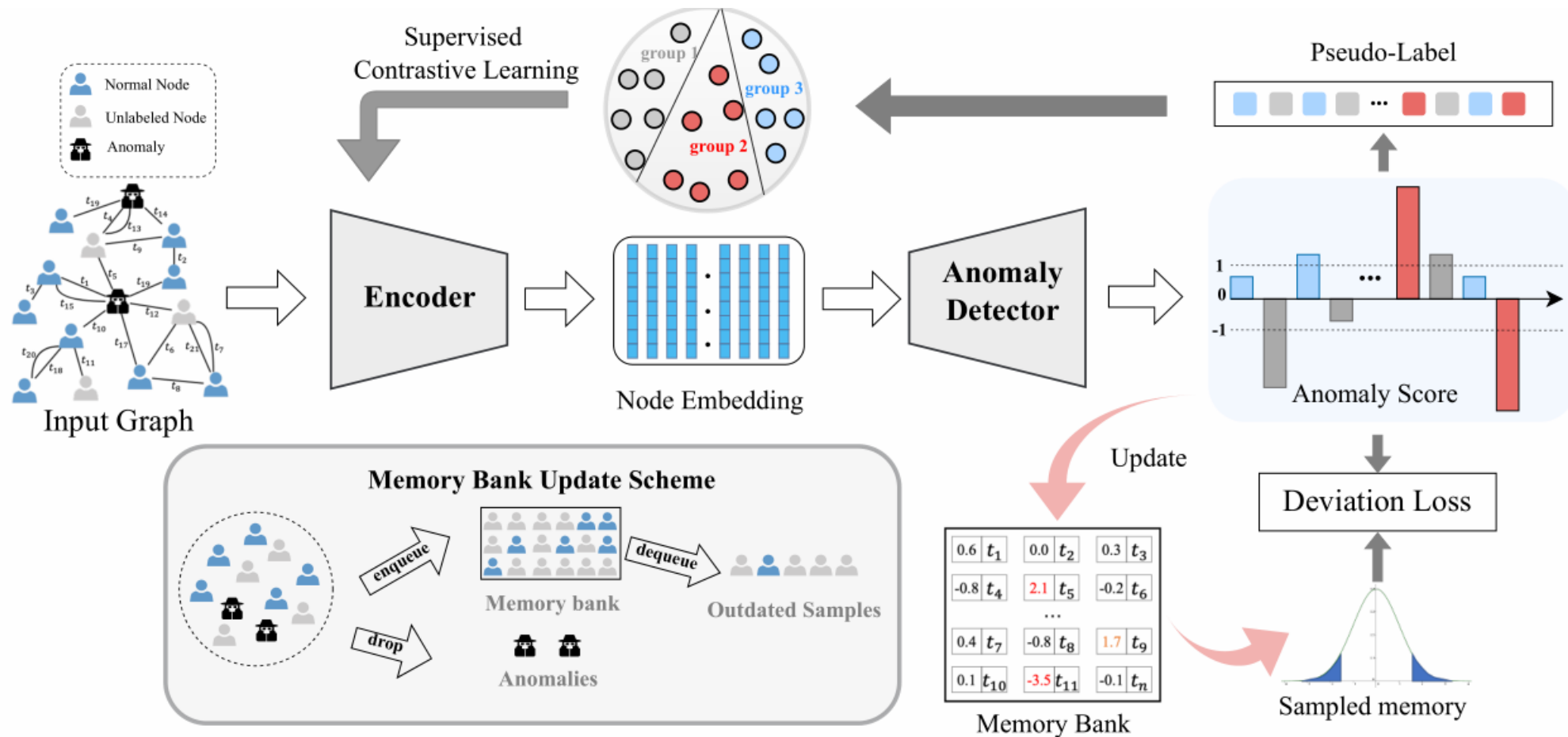
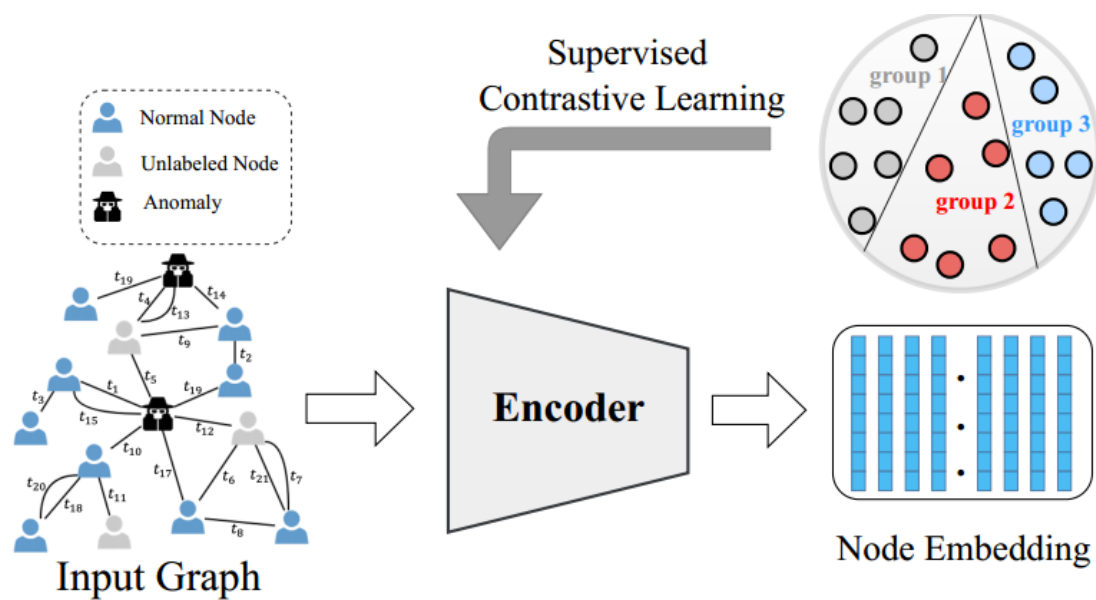


Figure 2: The proposed semi-supervised anomaly detection framework. SAD consists of four main components: the temporal graph encoder, the anomaly detector, the time-equipped memory bank, and the supervised contrastive learning module.

## Method



### PRELIMINARIES:

$$\mathcal{G} = (\mathcal{V}, \mathcal{E})$$

$$\mathcal{E} = \{\delta(t_1), \delta(t_2), \dots, \delta(t_m)\}$$

$$\delta(t) = (v_i, v_j, t, x_{ij})$$

### Deviation Networks with Memory Bank:

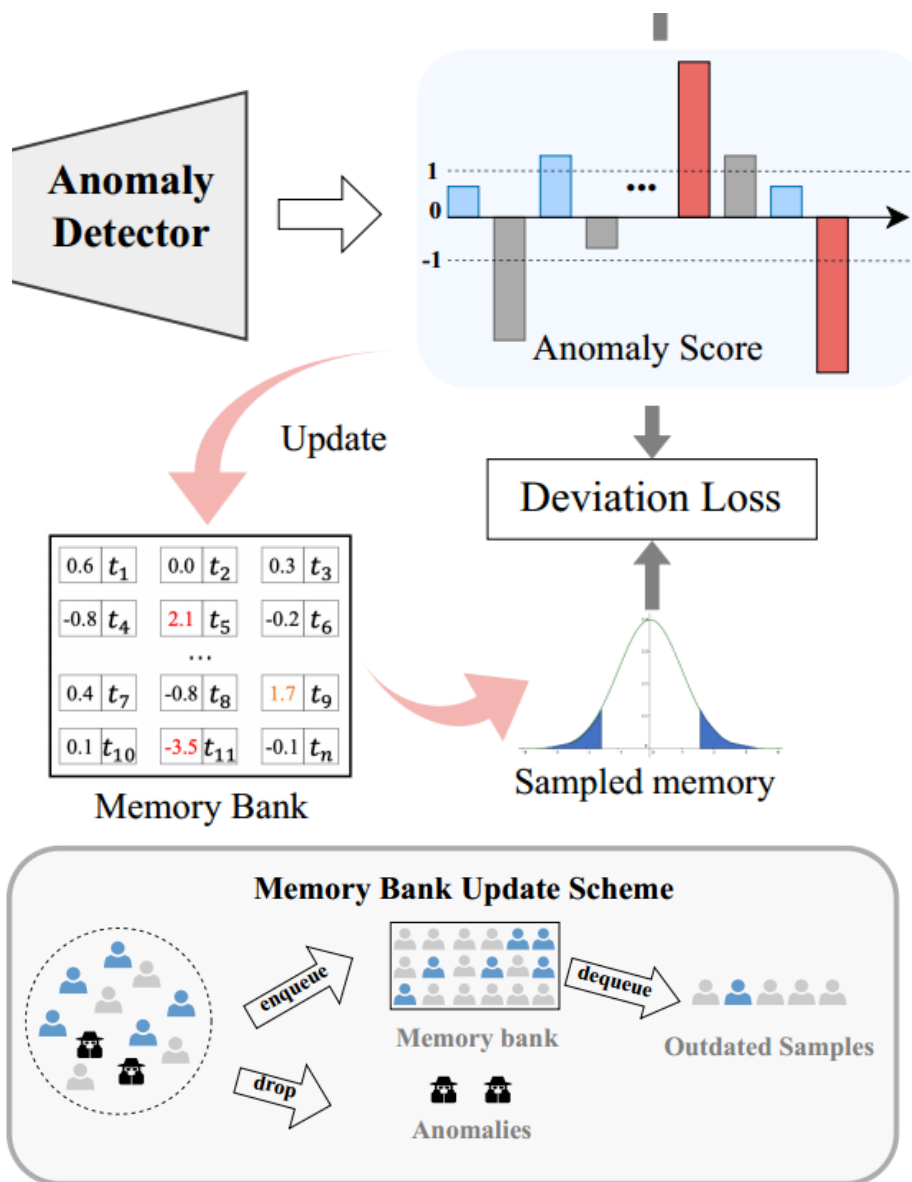
$$\mathbf{h}_{N_i}^{(k)}(t) = \text{AGG}^{(k)} \left( \left\{ (\mathbf{h}_j^{(k-1)}(t), x_{ij}, \phi(\Delta t)) : v_j \in \mathcal{N}(v_i, t) \right\} \right),$$

$$\mathbf{h}_i^{(k)}(t) = \text{COMBINE}^{(k)} \left( \mathbf{h}_i^{(k-1)}(t), \mathbf{h}_{N_i}^{(k)}(t) \right),$$

$$\Delta t = t - t_{ij}$$

(1)

$$z_i(t) = \mathbf{h}_i^{(K)}(t)$$



## Method

### Anomaly Detector:

$$s_i(t) = f_{\theta_a}(z_i(t)) = \mathbf{W}_2 \cdot \text{ReLU}(\mathbf{W}_1 \cdot z_i(t) + \mathbf{b}_1) + \mathbf{b}_2, \quad (2)$$

### Memory bank:

$$m = s_i(t), \quad \text{if } y_i(t) = 0 \text{ or } -1 \quad (3)$$

$$m = (s_i(t), t), \quad \text{if } y_i(t) = 0 \text{ or } -1 \quad (4)$$

### Deviation loss:

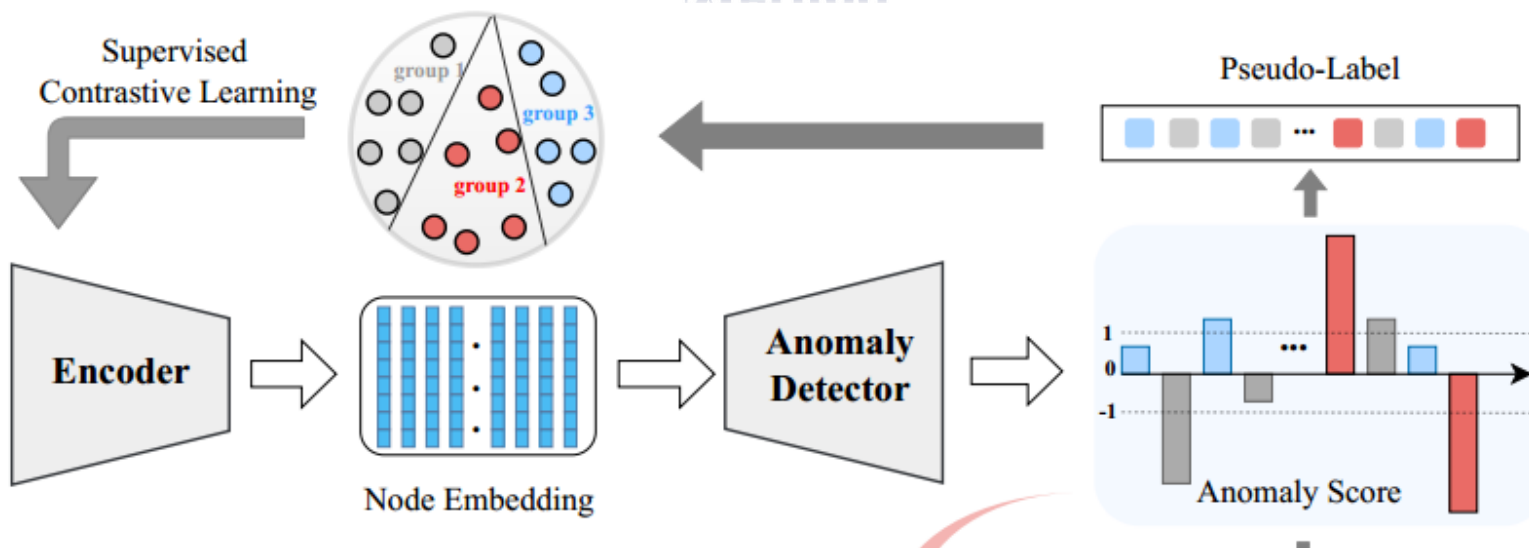
$$\mu_r(t) = \frac{1}{k} \sum_{i=1}^k w_i(t) \cdot r_i \quad (5)$$

$$\sigma_r(t) = \sqrt{\frac{\sum_{i=1}^k w_i(t) \cdot (r_i - \mu_r(t))^2}{k - 1}}$$

$$dev(v_i, t) = \frac{s_i(t) - \mu_r(t)}{\sigma_r(t)}. \quad (6)$$

$$\mathcal{L}^{dev} = (1 - y_i(t)) \cdot |dev(v_i, t)| + y_i(t) \cdot \max(0, m - |dev(v_i, t)|), \quad (7)$$

## Method



### Contrastive Learning for Unlabeled Samples:

$$\mathcal{L}_i^{scl} = \frac{-1}{N-1} \sum_{j, j \neq i}^N 1_{\Delta d_{ij} < 1} \cdot \frac{1}{1 + \Delta d_{ij}}$$

$$\ln \frac{\exp(z_i(t_i) \cdot z_j(t_j) / \tau)}{\sum_{k, i \neq k}^N \exp(z_i(t_i) \cdot z_k(t_k) / \tau)}$$

$$\Delta d_{ij} = |dev(v_i, t_i) - dev(v_j, t_j)|$$

### Learning procedure:

$$(8) \quad \arg \min_{\theta_{enc}, \theta_{ano}} \mathcal{L}^{dev}(\theta_{enc}, \theta_{ano}) + \alpha \mathcal{L}^{scl}(\theta_{enc}), \quad (9)$$

$$\arg \min_{\theta_{enc}, \theta_{ano}, \theta_{pro}} \mathcal{L}^{sup}(\theta_{pro}) + \alpha \mathcal{L}^{dev}(\theta_{enc}, \theta_{ano}) + \beta \mathcal{L}^{scl}(\theta_{enc}), \quad (10)$$

# Experiments

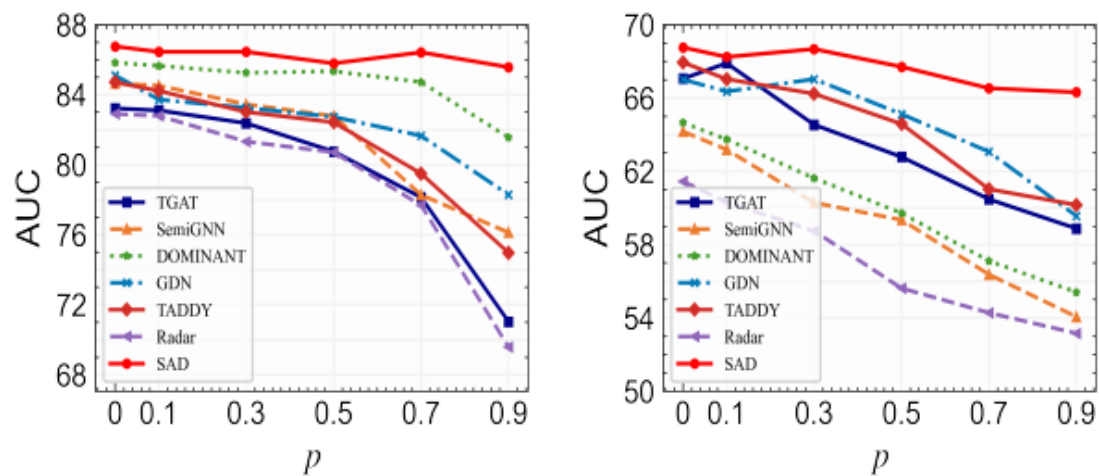
	Wikipedia	Reddit	Mooc	Alipay
#Nodes	9,227	10,984	7,074	3,575,301
#Edges	157,474	672,447	411,749	53,789,768
#Edge features	172	172	4	100
#Anomalies	217	366	4,066	24,979
Timespan	30 days	30 days	30 days	90 days
Pos. label meaning	posting banned	editing banned	dropping out	fraudster
Chronological Split	70%-15%-15%	70%-15%-15%	70%-15%-15%	70%-15%-15%

Table 1: Statistics of datasets.

Methods	Wikipedia	Reddit	Mooc	Alipay
TGAT	83.23 $\pm$ 0.84	67.06 $\pm$ 0.69	66.88 $\pm$ 0.68	92.53 $\pm$ 0.93
TGN	84.67 $\pm$ 0.36	62.66 $\pm$ 0.85	67.07 $\pm$ 0.73	92.84 $\pm$ 0.81
Radar	82.91 $\pm$ 0.97	61.46 $\pm$ 1.27	62.14 $\pm$ 0.89	88.18 $\pm$ 1.05
DOMINANT	85.84 $\pm$ 0.63	64.66 $\pm$ 1.29	65.41 $\pm$ 0.72	91.57 $\pm$ 0.93
SemiGNN	84.65 $\pm$ 0.82	64.18 $\pm$ 0.78	64.98 $\pm$ 0.63	92.29 $\pm$ 0.85
GDN	85.12 $\pm$ 0.69	67.02 $\pm$ 0.51	66.21 $\pm$ 0.74	93.64 $\pm$ 0.79
TADDY	84.72 $\pm$ 1.01	67.95 $\pm$ 0.94	68.47 $\pm$ 0.76	93.15 $\pm$ 0.88
SAD	<b>86.77 <math>\pm</math> 0.24</b>	<b>68.77 <math>\pm</math> 0.75</b>	<b>69.44 <math>\pm</math> 0.87</b>	<b>94.48 <math>\pm</math> 0.65</b>

Table 2: Overall performance of all methods in terms of AUC on dynamic node classification tasks. Means and standard deviations were computed over 10 runs.

# Experiments



(a) Wikipedia

(b) Reddit

Figure 3: Dynamic node classification task results under different drop ratios  $p$  on Wikipedia and Reddit, respectively.

	Wikipedia	Reddit	Mooc
TGAT	$80.76 \pm 2.30$	$62.79 \pm 3.42$	$64.04 \pm 1.02$
w/dev	$82.45 \pm 0.64$	$64.15 \pm 2.93$	$65.33 \pm 1.67$
w/mem	$85.20 \pm 1.30$	$66.96 \pm 1.51$	$67.25 \pm 0.75$
w/time	$85.44 \pm 0.75$	$66.78 \pm 1.98$	$67.53 \pm 0.93$
w/scl	<b><math>85.80 \pm 1.32</math></b>	<b><math>67.71 \pm 0.75</math></b>	<b><math>67.57 \pm 0.54</math></b>

Table 3: Results of the ablation study on the dynamic node classification task under the label-dropping ratio of 0.5.



# Experiments

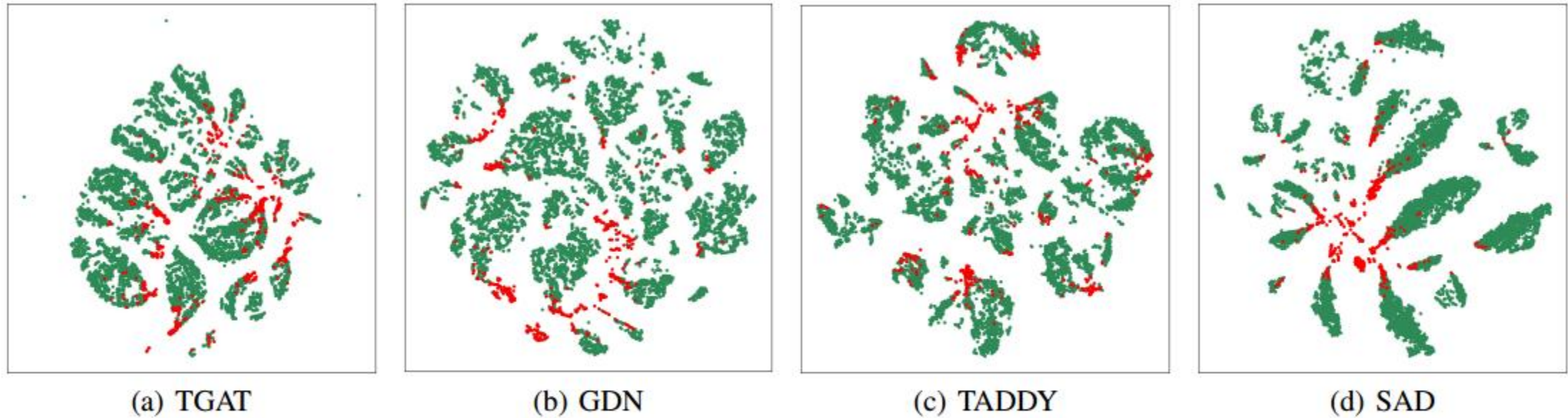


Figure 4: Visualization of the learned node embeddings w.r.t. different methods on Alipay. The red and green points represent the abnormal and normal samples, respectively.